Analysis of Inductively Coupled RFID Marker Localization Methods

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Abstract — The presented paper is focused on analysis of two methods of marker localization. The markers are passive RFID transponders (without or with identification chip) consisting of tuned LC circuit and being used to mark and trace underground networks such as cables and pipes. Localization of the marker is based on evaluation of signal amplitude received from the excited marker, i.e. it is RSSI based localization method. The excitation of marker can be periodically repeated or continuous. In the first case the localization process consists of two stages – excitation and receiving of marker damped oscillations, in the second case the amplitude of continuously generated excitation signal is decreased by vicinity of the marker. Both localization methods are mathematically analyzed by modeling of their circuits using differential equations. The results of analysis are used to compare both methods and to evaluate their suitability for practical utilization.

I. INTRODUCTION

INDUCTIVELY coupled RFID (Radio Frequency Identification) systems [1] are now being widely used in many industrial applications. For example, the marking of goods by RFID technology enables the traceability of goods which is helpful to control the whole logistic chain from production to sale. In addition to these applications, the RFID transponders are being used for marking of underground facilities location. Such RFID transponders are called “markers”. The marker is a passive RFID transponder consisting of a tuned LC circuit without identification chip (1-bit) or with identification chip tuned on low frequency in 77 kHz – 170 kHz band.

For localization of some older underground facilities (cables, pipes etc.) a signal can be injected into their continual metal conductor and this signal can then be received on terrain surface and the cable or pipe can be traced. Today’s underground facilities are mostly constructed from plastic material so this simple localization and tracing method cannot be used, therefore in this case the marking of underground objects by RFID markers is the only useable method.

The unknown position of marker under the terrain surface can be estimated by a localization device (locator). Moreover, the depth of marker can be estimated by RSSI (Received Signal Strength Indication) similarly as described in [2], [3]. In [4] the authors describe marker localization methods based on marker damped oscillations and on continuous generating of electromagnetic waves. This work extends the analyses of RSSI based marker localization methods. The method based on damped oscillations of marker is extended by introduction of separate damping and sensing resistors and the analysis of method based on continuous marker excitation is done by applying differential equations instead of algebraic equations to analyze the transient phenomena in sensing circuit.

II. RELATED WORKS

The localization of moving underground objects (for example animals) based on inductive coupling is described in [5]. This application assumes the use of sensor network consisting of transmitting coils fixed on terrain surface and the moving underground object equipped with receiver collects data transmitted from these coils.

Indoor localization based on triaxial coils applied in both transmitter and receiver with very low working frequency 2.5 kHz is published in [6]. Low frequency magnetic field is suitable for underground localization purposes, too, because it is not affected by ground properties.

Another approach is presented in [7]. This work assumes localization based on UHF RFID tags in mining industry, but it is performed in mining tunnels and localization from the terrain surface is not assumed so the UHF signals do not propagate through layer of ground.

III. MUTUAL INDUCTANCE

An important quantity in the models presented in next chapters is the mutual inductance M between marker and locator coils which depends on the geometrical arrangement of coils according to equation [1], [4], [8]:

\[
M = \frac{\sqrt{L_1 L_2 r_0^3 r_1^3 \cos \Theta}}{r_0^2 r_1 \left(r_0^2 + x^2\right)^{3/2}}
\]
where \( r_R \) is radius of RFID locator antenna coil, \( r_T \) is radius of marker coil, \( x \) is distance between the locator antenna and the marker and \( \theta \) is the angle between coil of locator antenna and marker coil (note that if \( \theta=0^\circ \) then coils are parallel).

IV. MATHEMATICAL MODEL BASED ON DAMPED OSCILLATION

This principle of localization assumes that the localization device periodically excites the marker LC circuit and in the pauses between excitation periods the response from marker in form of its damped oscillations is received. The simple model with one resistor was analyzed in [4]. In this chapter a more complex model with separate damping and sensing resisters will be analyzed. The first resistor \( R_D \) is used for fast damping of locator \( L_R C_R \) circuit damped oscillations and its value was calculated from equation (2). The second resistor \( R_M \) is used for current sensing in the receiving stage of localization. The model is shown in Fig. 1.

\[
R_D = 2 \sqrt{\frac{r_K}{C_R} - R_R}
\]

For this model the next system of equations (3) can be derived

\[
L_x \frac{dx(t)}{dt} + \left[ (1 - \text{MOD}(t)) R_D + \text{MER}(t) R_M \right] x(t) + R_x y(t) + \int c_x(t) d\tau = M \frac{dx(t)}{dt} \]

The modulation function \( \text{MOD}(t) \) is given by equation (4) and the sensing (measuring) resistor \( R_M \) is switched by function \( \text{MER}(t) \) given by the equation (5)

\[
\text{MOD}(t) = \frac{\text{Sign} \left( -\sin \left( \frac{2\pi f(t - \Delta T)}{250} \right) \right) + 1}{2}
\]

\[
\text{MER}(t) = \frac{\text{Sign} \left( -\sin \left( \frac{2\pi f(t - \Delta T)}{250} \right) \right) + 1}{2}
\]

The used values of \( R_R, L_R, C_R \) and \( R_T, L_T, C_T \) are listed in the next table:

<table>
<thead>
<tr>
<th></th>
<th>( R_R )</th>
<th>( L_R )</th>
<th>( C_R )</th>
<th>( R_T )</th>
<th>( L_T )</th>
<th>( C_T )</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>15.7 ( \Omega )</td>
<td>1 mH</td>
<td>1.621 nF</td>
<td>7.85 ( \Omega )</td>
<td>1 mH</td>
<td>1.621 nF</td>
</tr>
</tbody>
</table>

Note that the values of \( L_R, C_R \) and \( L_T, C_T \) were selected so that the corresponding resonant frequencies are \( f_R = f_L = 125 \text{ kHz} \).

The radiiuses of both coils used in numerical calculations are \( r_R = r_L = 0.1 \text{ m} \), distance between them is \( x = 0.4 \text{ m} \) and the angle \( \theta = 0^\circ \). Corresponding mutual inductance \( M \) is then calculated from (1). Amplitude of the excitation signal is \( U_i = 10 \text{ V} \), its frequency \( f \) is 125 kHz.

The damping resistor \( R_D = 1533 \text{ } \Omega \) calculated from (2) in this case ensures the minimum time of \( L_R C_R \) transient

\[
\text{MOD}(t) = \frac{\text{Sign} \left( -\sin \left( \frac{2\pi f(t - \Delta T)}{250} \right) \right) + 1}{2}
\]
response. The used values of the measuring resistor are $R_M = 100 \, \Omega$ for comparison with the results obtained in [4] and $R_M = 1 \, \Omega$ to maximize the current response $i_1(t)$ from marker.

The time course of the current $i_1(t)$ for model of marker localization with two resistors is shown in Fig. 2 and Fig. 3 for $R_D = 1533 \, \Omega$, $R_M = 100 \, \Omega$ and $R_M = 1 \, \Omega$, respectively.

Moreover, the dependence of maximum current amplitude $I_{1,\text{Max}}$ on the distance $x$ was calculated for this model and it is shown in Fig. 4. Note that the current maximum was calculated in the time interval after the transients of the excitation current decay. For comparison of the presented analysis results and the results from simplified model calculated in [4] the case when $R_D = R_M$ was calculated, too. This case is identical with the simplified model and the comparison is shown in Fig. 4.

The measuring resistor $R_M$ influences the maximum current amplitude $I_{1,\text{Max}}$ because this resistors acts as additional damping resistor for $L_R C_R$ circuit so that the ideal situation is when $R_M \to 0$.

![Fig. 2 Time course of the current $i_1(t)$ for $R_D = 1533 \, \Omega$ and $R_M = 100 \, \Omega$.](image)

![Fig. 3 Time course of the current $i_1(t)$ for $R_D = 1533 \, \Omega$ and $R_M = 1 \, \Omega$.](image)

![Fig. 4 Maximum amplitude of current response from marker with nominal resonant frequency $f = 125 \, \text{kHz}$ for two resistor model.](image)

![Fig. 5 Maximum amplitude of current response from marker for damped oscillation model.](image)

![Fig. 6 Dependence of maximum current amplitude on the measuring resistor $R_M$ for distance $x = 0.4 \, \text{m}$.](image)

V. MATHEMATICAL MODEL BASED ON CONTINUOUS EXCITATION OF MARKER

This localization principle is used when the RFID locator continuously generates the magnetic field by its antenna coil $L_R$. The amplitude of current in locator circuit is then
influenced by resonant circuit of marker so that the steady state current amplitude in locator circuit decreases if the marker is nearby.

The model is derived from the previous case by eliminating the switches. Schematic diagram of this model is shown in Fig. 7. In dependence on the distance \( x \) between coils the marker resonant circuit influences the amplitude of current \( i(1) \) in locator antenna circuit.

This model can be analyzed by using of complex impedances of its components as it was performed in [4]. But such analysis did not show the transient phenomena in locator circuit and the results give only steady state solution. Therefore new model based on differential equations was created.

This model can be described by the following system of differential equations:

\[
\begin{align*}
\frac{d}{dt} i_1(t) + R_d i_1(t) + \frac{1}{C_x} \int_0^t i_1(\tau) d\tau - M \frac{di_2(t)}{dt} &= u(t) \\
\frac{d}{dt} i_2(t) + R_f i_2(t) + \frac{1}{C_T} \int_0^t i_2(\tau) d\tau - M \frac{di_1(t)}{dt} &= 0
\end{align*}
\]  

The signal source in Fig. 7 is harmonic as defined by (6). Similar as in previous chapter the system of integro-differential equations (9) was transformed by substitution \( x_1(t)=i_1(t) \), \( x_2(t)=di_1(t)/dt \), \( x_3(t)=i_2(t) \), \( x_4(t)=di_2(t)/dt \), \( \omega=2\pi f \). Then we get the 1\textsuperscript{st} order system of differential equations (10) which can be easily solved by standard mathematic software.

\[
\begin{align*}
\frac{dx_1(t)}{dt} &= x_2(t) \\
\frac{dx_2(t)}{dt} &= a_1 x_1(t) + a_2 x_2(t) + a_3 x_3(t) + a_4 x_4(t) + a_5 \omega U_1 \cos(\omega t) \\
\frac{dx_3(t)}{dt} &= x_4(t) \\
\frac{dx_4(t)}{dt} &= b_1 x_1(t) + b_2 x_2(t) + b_3 x_3(t) + b_4 x_4(t) + b_5 \omega U_1 \cos(\omega t)
\end{align*}
\]

where individual coefficients are given by (11). Note that these coefficients are different from the coefficients given by (8).

\[
\begin{align*}
a_1 &= \frac{L_f}{C_x(M^2 - L_f L_T)} \\
b_2 &= \frac{R_f M}{M^2 - L_f L_T} \\
a_3 &= \frac{M}{C_T(M^2 - L_f L_T)} \\
b_4 &= \frac{L_f R_f}{M^2 - L_f L_T} \\
a_5 &= \frac{L_f}{M^2 - L_f L_T} \\
b_5 &= \frac{M}{M^2 - L_f L_T}
\end{align*}
\]  

In this case the detection of marker vicinity is more complicated as in the previous chapter because there is not the time stage in which only the response from excited marker can be received but the excitation signal in locator circuit is always present. The symptom of marker vicinity is decreasing of steady state current amplitude in locator circuit. When the distance between marker and locator is big (\( x \to \infty \)) then the mutual inductance calculated from (1) is very small (\( M \to 0 \)). In this case the current \( i(1) \) has maximum value \( I_{\text{max}} \), which is measured in steady state after the time \( t=2.5 \text{ ms} \). The marker vicinity then causes current drop \( \Delta I_1 \) (12) which can be calculated as difference between steady value of current \( i(1) \) (see Fig. 8) and its maximum \( I_{\text{max}} \) measured in the same time point when no marker is nearby the locator.

\[\Delta I_1 = I_{\text{max}} - I_1 \]  

The time course of current \( i_1(t) \) in the RFID locator circuit (Fig. 8) was numerically calculated from the system (10) for the same parameters as used in previous chapter. The dependence of current drop \( \Delta I_1 \) versus distance \( x \) is shown in Fig. 9.

\[
\begin{align*}
\frac{dx_1(t)}{dt} &= x_2(t) \\
\frac{dx_2(t)}{dt} &= a_1 x_1(t) + a_2 x_2(t) + a_3 x_3(t) + a_4 x_4(t) + a_5 \omega U_1 \cos(\omega t) \\
\frac{dx_3(t)}{dt} &= x_4(t) \\
\frac{dx_4(t)}{dt} &= b_1 x_1(t) + b_2 x_2(t) + b_3 x_3(t) + b_4 x_4(t) + b_5 \omega U_1 \cos(\omega t)
\end{align*}
\]

Fig. 7 Model of localization based on continuous excitation

Fig. 8 The time course of current \( i_1(t) \), distance \( x=0.3 \text{ m} \)
Another criterion for evaluation of presented localization methods is based on their sensitivity to the marker vicinity. From comparison in Fig. 10 the second method seems to be more sensitive to the marker vicinity. Because the markers are typical near field application, the current amplitude in both cases decreases very rapidly when the distance between marker and locator increases.

The next research will be focused on the design of hardware needed to perform series of measurements so that the results of performed analyses will be compared with real measured data.

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